Name: $\qquad$

Age: $\qquad$ Yrs $\qquad$ Mths

ST PAUL'S
$\qquad$

FIRST YEAR ENTRANCE EXAMINATION

## MATHEMATICS

## Paper 1

## 35 minutes

## PLEASE READ THESE INSTRUCTIONS VERY CAREFULLY

Use a pencil. No calculators, protractors or rulers are allowed.
There are two sections. The invigilator will tell you when you should begin Section 2.
Section 1 is multiple choice and does not require any workings.
Show all your workings in Section 2 and write your answers on the lines provided.

## Please do not rub out your workings.

If you cannot do a question, leave it and go on to the next one. Try again later.
You cannot ask a teacher for explanations.
If you finish before the end of 35 minutes go back and check your answers. Try to complete any questions you have left out.

## Section 1 - Questions

1
Calculate 15.05-14.84
A 0.21
B 0.39
C 0.29
D 0.31
E 0.1

2 Calculate $31.6 \times 7$
A 220.5
B 221.2
C 223
D 224
E 230

3
Calculate 60\% of 765
A 465
B 459
C 455
D 440
E 435

4 Fill in the missing number: $\frac{1}{2}$ of $20=\frac{1}{4}$ of [ ]
A 40
B 35
C 30
D 25
E 24

5 Fill in the missing number: $0.627=0.6+0.02+$ $\qquad$
A 0.5
B 0.07
C 0.05
D 0.007
E 0.005

6
Circle the number closest in value to 0.1
A 0.02
B 0.08
C 0.13
D 0.2
E 0.9

A bag contains 20 marbles and weighs 42 g . The empty box weighs 12 g . Calculate the weight of one marble.
A 1 g
B $\quad 1.2 \mathrm{~g}$
C $\quad 1.5 \mathrm{~g}$
D 1.6 g
E 1.8 g

8
Calculate $848 \div 16$
A 40
B 53
C 60
D 54
E 106

9
Calculate $11 \%$ of 30,500
A 3885
B 3355
C 3835
D 3585
E 3850

10 A quarter of a third of a number is one. What is the number?
A 10
B 12
C 14
D 15
E 20

## Section 1 - Answers

## Circle a letter to indicate your answer.

## Question

| $\mathbf{1}$ | A | B | C | D |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2}$ | A | B | C | D | E |
| $\mathbf{3}$ | A | B | C | D | E |
| $\mathbf{4}$ | A | B | C | D | E |
| $\mathbf{5}$ | A | B | C | D | E |
| $\mathbf{6}$ | A | B | C | D | E |
| $\mathbf{7}$ | A | B | C | D | E |
| $\mathbf{8}$ | A | B | C | D | E |
| $\mathbf{9}$ | A | B | C | D | E |

## Section 2 - Questions

1. a) Billie bought a 1.5 kg leg of lamb for dinner.

However, she had not cooked a leg of lamb before so she looked it up in her recipe book.
It said that the cooking time (in minutes) for the leg of lamb is
" 50 times the weight (in kg ) plus an additional 32".
For how long, in hours and minutes, should Billie cook the lamb?

Answer $\qquad$ .hours. $\qquad$ minutes.

b) She also needs to roast some potatoes to accompany the lamb. She knows this will take 55 minutes.

Steaming some greens will take 8 minutes. If she wants to serve lamb, potatoes and greens together at 6 pm , at what time should she start cooking each of these?


Potatoes:


Greens:

2. (a) A train leaves London Waterloo for Exeter St David's at 11:35.

It calls at Clapham Junction, Salisbury and Yeovil Junction but at each of these stations the train is delayed by 5 minutes. According to the timetable the journey should take 3 hours and 42 minutes if the train is not delayed.

At what time does it arrive?

Answer

(b) Another train left London at 22:03 and arrived in Aberdeen at 06:18 the next day. How long did the journey take?
3. Write down two calculations with the same answer using the given numbers and symbols. You may use each number or symbol only once.
$\begin{array}{llllll}7 & 7 & 8 & 63 & - & \times\end{array}$


Answer ...Calculation 2

4. Below are four views of the same die.

Draw the correct missing face of the final view.

5. The sum of each two steps which are side by side gives the number above them.

For example, $13+28=41$
What number replaces the A?

6. In a class of 30 pupils, 20 like lemonade, 17 like strawberry milkshake and 11 like both. How many pupils:
(a) like only lemonade

(b) like neither

7. In the given grid, each unit represents 1 cm . Find the area of figure $A B C D$.

8. The average age of Sita, Vina, Aarti and Pooja is 17 years.

Aarti is 11 years old, Sita and Vina are the same age and Pooja is 3 years older than Sita and Vina. How old is Sita?
9. The following words have been written in number code where each letter is represented by one digit. Match up the following words with the code numbers.
stops
posts
strop
spots
ports
sport

| Number code | Fill in the word |
| :---: | :---: |
| 75386 |  |
| 68576 |  |
| 67538 |  |
| 67586 |  |
| 75686 |  |
| 68357 |  |

10. Fifteen red snooker balls are placed in the frame as shown.


A second layer is placed on top of them, so that they rest in the spaces.
This is followed by more layers until there is a single ball at the top.
(a) How many layers are there?

(b) How many balls are needed to make this pyramid?

$\qquad$
$\qquad$

# FIRST YEAR ENTRANCE EXAMINATION 

## MATHEMATICS

## Paper 2

## 40 minutes

## PLEASE READ THESE INSTRUCTIONS VERY CAREFULLY

Use a pencil. No calculators, protractors or rulers are allowed.

There are 5 questions.

Show all your working in the spaces provided and write your answers on the lines provided.

## Please do not rub out your working.

If you cannot do a question, leave it and go on to the next one.
Try again later.

Do not ask a teacher to explain a question to you.

If you finish before the end of 40 minutes go back and check your answers and try to fill in any answers you have left out.

1. Using 1 s and 2 s , there is only one way to represent the value 1 .

However, there are two ways of making the value 2 :

$$
1+1 \text { or } 2 \text {. }
$$

There are three ways of adding up an ordered combination of 1 s and 2 s to make 3 :

```
1+1+1 or 2+1 or 1+2
```

Notice that order is important here!
a) How many ways can you add up an ordered combination of 1 s and 2 s to make 4?

Answer

b) How many ways can you add up an ordered combination of 1 s and 2 s to make 5 ?

c) By considering these results, prove that there are exactly 21 ways you can add up an ordered combination of 1 s and 2 s to make 7 .
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
2.

You are given that angles which form a Z-shape within parallel lines are equal.

a) Now, using the diagram below, explain how you know the angles in a triangle sum to $180^{\circ}$.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

$\qquad$
$\qquad$
b)

What is the sum of the six shaded angles?


Answer $\qquad$ $\theta$
3. A top sprinter runs 100 metres in 10 seconds.
(a) What is his speed in metres per second?
(In other words, how many metres does he run each second)?

## Answer

$\qquad$ .metres per second.

To convert a speed from metres per second to miles per hour, multiply by 9 and divide by 4 .
(b) A car is travelling at 20 metres per second. Change that speed to miles per hour.

Answer .miles per hour.
(c) How would you convert a speed from miles per hour into metres per second?

## Answer

$\qquad$
(d) My new garden blower (for "sweeping" up leaves) blows at 180 miles per hour. How fast is that in metres per second?
4. Here is how you can solve problems like the example below:

Example: What's my number?
When it is divided by 3 it leaves remainder 2 and when it is divided by 5 it leaves remainder 4. The numbers that leave remainder 2 when divided by 3 are the numbers in the sequence

$$
2,5,8,11,14, \ldots
$$

The numbers that leave remainder 4 when divided by 5 are the numbers in the sequence

$$
4,9,14,19,24, \ldots
$$

Look at the sequences for a number they have in common (i.e. a number in both sequences). The smallest possible solution is 14 , but the sequences also have the numbers $29,44,59, \ldots$ in common, so there is more than one possible solution.
Use the approach described above to solve the questions below:
(a) A box contains more than 25 but less than 40 tennis balls.

When the balls are counted in threes there is one left over.
When counted in fives there are two left over. How many balls are in the box?
(b) There are between 330 and 380 people at a concert. When they form groups of five then 3 people are left over. When they form groups of seven then 5 people are left over. When they form groups of eleven then 7 people are left over. How many people are at the concert?
5. You are told that $O_{n}$ is 'the value of the first $n$ odd numbers multiplied together' and that $E_{n}$ is 'the value of the first $n$ even numbers multiplied together'. For example,

$$
\begin{gathered}
O_{3}=1 \times 3 \times 5=15 \\
O_{5}=1 \times 3 \times 5 \times 7 \times 9=945 \\
E_{6}=2 \times 4 \times 6 \times 8 \times 10 \times 12=46,080
\end{gathered}
$$

(a) Calculate $O_{6}$

Answer $\qquad$
(b) What is the remainder when $O_{50}$ is divided by 15 ?
(c) What is the remainder when $O_{100}$ is divided by 2 ?

## Answer

(d) What is the remainder when $\mathrm{E}_{100}$ is divided by 3 ?

## Answer



You are told that $n!$ is 'the value of the first $n$ counting numbers multiplied together'. For example,

$$
\begin{gathered}
1!=1 \\
2!=1 \times 2=2 \\
3!=1 \times 2 \times 3=6
\end{gathered}
$$

(e) Use your answer to (a) to calculate 12!

## Answer

(f) What is the remainder when $1!+2!+3!+4!+5!+6!+7!+8!$ is divided by 5 ?
$\qquad$

## END OF SECTION 2

NOW GO BACK AND CHECK YOUR ANSWERS

